



# Evolving Fuzzy Neural Networks by Particle Swarm Optimization with Fuzzy Genotype Values

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**Abstract:** Particle swarm optimization (PSO) is a well-known instance of swarm intelligence algorithms and there have been many researches on PSO. In this paper, the author proposes an extension of PSO for solving fuzzy-valued optimization problems. In the proposed extension, genotype values (i.e. values in particle position vectors) are not real numbers but fuzzy numbers. Search processes in PSO are extended so that PSO can handle genotype instances with fuzzy numbers. The proposed method is experimentally applied to evolution of neural networks with fuzzy weights and biases. Experimental results showed that fuzzy neural networks evolved by the proposed method could model hidden target fuzzy functions despite the fact that no training data was explicitly provided.

**Keywords:** Evolutionary algorithm, Swarm intelligence, Particle swarm optimization, Fuzzy number, Feedforward neural network, Neuroevolution

## 1. INTRODUCTION

A multi-layered feed forward neural network (NN) with fuzzy-valued weights and biases was proposed in literature [1]. The fuzzy NN (FNN) approximately models a fuzzy function  $Y = F(\mathbf{x})$ , where  $Y$  is a fuzzy number and  $\mathbf{x}$  is a real vector, by learning given data  $(\mathbf{x}_1, Y_1)$ ,  $(\mathbf{x}_2, Y_2)$ , .... The FNN can learn the data in which  $Y_1, Y_2, \dots$  include both of real numbers and fuzzy numbers, because a real number can be specified as a fuzzy number with zero width (i.e., with the same value of upper and lower limits). As the learning method for the FNNs, a supervised learning method was also proposed [1] which is an extension of the traditional back propagation (BP), but a method that does not require training data has yet not been proposed.

Besides, evolutionary algorithms have recently been applied to the reinforcement training of NNs, known as neuroevolution (NE) [2-5]. In NE, weights and biases are tuned by evolutionary operations, not by the BP algorithm. Because NE does not utilize BP, NE does not require errors between NN output values and their target signals but only require each NN to be ranked based on the performance of the NN for a given task. Thus, NE is applicable to problems in which the error function is difficult or impossible to be determined, such as controlling autonomous robots. EAs have been applied to

NE of traditional NNs with real-valued weights and biases, where the genotypes (chromosomes) consist of real numbers or bit strings that encode real numbers. The ordinary EAs have not employed fuzzy numbers as their genotype values because their evolutionary operations are designed to handle genotypes with crisp values and thus the operations cannot handle genotypes with fuzzy values.

The author previously proposed an extension of genetic algorithm which can handle fuzzy-valued genotypes [6]. In this paper, the author proposes a similar extension of another EA, particle swarm optimization (PSO). PSO [7,8] is a well-known instance of the EAs (more specifically, an instance of swarm intelligence algorithms [9]). Researchers have applied PSO to the training of NNs [10-19], but the NNs are traditional ones with real-valued weights and biases. On the contrary, the extended PSO proposed in this paper can be applied directly to fuzzy optimization problems by employing fuzzy variables in a fuzzy optimization problem as genotype values. The author experimentally applies the proposed method (fuzzy-valued PSO: FPSO) to reinforcement training of FNNs and compares the experimental result with the result by the previously proposed fuzzy-valued GA [6].

## 2. NEURAL NETWORKS WITH FUZZY WEIGHTS AND BIASES

The FNN employed in this research is the same as in the literature [1], which is a three-layered feed forward NN with fuzzy weights and biases. Fig.1 shows its structure. An FNN receives an input real vector  $\mathbf{x}$  and calculates its output fuzzy value  $O$  (for simplicity, the output layer includes a single unit) as follows [1]:

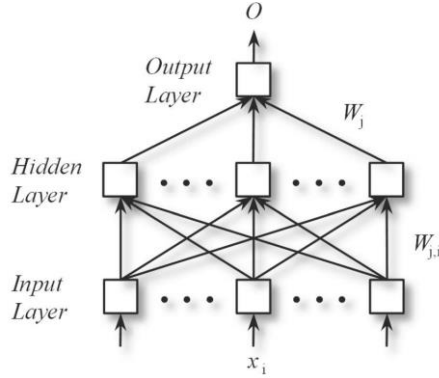


Figure 1. Neural network with fuzzy weights and biases [1].

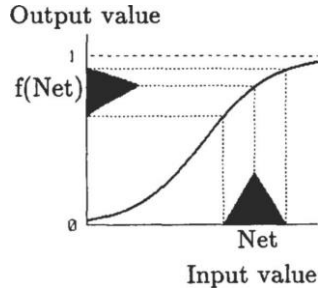


Figure 2. Input-output relation of each unit in the hidden and output layers [1].

Input Layer:

$$o_i = x_i. \quad (1)$$

Hidden Layer:

$$Net_j = \sum_i W_{j,i} o_i + \Theta_j, \quad (2)$$

$$O_j = f(Net_j). \quad (3)$$

Output Layer:

$$Net = \sum_j W_j O_j + \Theta, \quad (4)$$

$$O = f(Net). \quad (5)$$

In (1)-(5),  $x_i$  and  $o_i$  are real values, while  $Net_j$ ,  $Net$ ,  $W_{j,i}$ ,  $W_j$ ,  $\Theta_j$ ,  $\Theta$ ,  $O_j$  and  $O$  are fuzzy values.  $f(x)$  is the unit activation function which is typically the sigmoidal one:  $f(x) = 1/(1 + e^{-x})$ .  $f(x)$  maps a fuzzy input number to a fuzzy output number as illustrated in Fig.2.

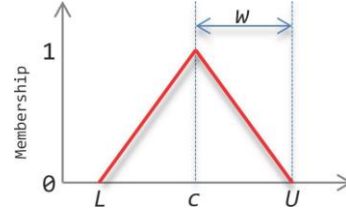


Figure 3. Symmetric triangular fuzzy number and its real-valued parameters [6].

The feed-forward calculation of the FNN is based on the extension principle [20] and the interval arithmetic [21] (for more detail, see the literature [1]). Let us denote two closed intervals  $A$  and  $B$ , where  $A = [a^L, a^U]$  and  $B = [b^L, b^U]$ . In this case,

$$\begin{aligned} A + B &= [a^L, a^U] + [b^L, b^U] \\ &= [a^L + b^L, a^U + b^U]. \end{aligned} \quad (6)$$

$$\begin{aligned} k \cdot A &= k \cdot [a^L, a^U] \\ &= [ka^L, ka^U], \text{ if } k \geq 0, \text{ else } [ka^U, ka^L]. \end{aligned} \quad (7)$$

$$\begin{aligned} A \cdot B &= [a^L, a^U] \cdot [b^L, b^U] \\ &= [\min(a^L b^L, a^L b^U, a^U b^L, a^U b^U), \\ &\quad \max(a^L b^L, a^L b^U, a^U b^L, a^U b^U)]. \end{aligned} \quad (8)$$

The FNN includes  $mn + m$  weights (i.e.,  $mn$  weights between  $n$  input units and  $m$  hidden units, and  $m$  weights between  $m$  hidden units and an output unit) and  $m + 1$  biases (= the total number of units in the hidden and output layers). Thus, the FNN includes  $mn + 2m + 1$  fuzzy variables in total. The FPSO handles these fuzzy variables as a genotype  $\mathbf{X} = (X_1, X_2, \dots, X_D)$  where  $X_i$  is a fuzzy number and  $D = mn + 2m + 1$ .

Suppose each  $X_i$  is a symmetric triangular fuzzy number (Fig.3) as in [6]. In this case,  $X_i$  can be specified by its upper and lower limits or by its center and width (radius):  $X_i = [x_i^L, x_i^U]$  or  $X_i = (x_i^C, x_i^w)$  where  $x_i^L$ ,  $x_i^U$ ,  $x_i^C$ ,  $x_i^w$  denote the upper, lower, center and width of  $X_i$  respectively.

## 3. FUZZY PSO: PSO WITH FUZZY-VALUED GENOTYPES

The proposed FPSO consists of the same processes as those in the ordinary PSO with real-valued genotypes. Processes of initialization of population, fitness evaluation and updates of particles are extended so that these processes can handle fuzzy-valued genotypes.

### A. Initialization of Population

In the initialization process,  $\mathbf{X}_1, \mathbf{X}_2, \dots, \mathbf{X}_P$  are randomly initialized where  $P$  is the population size. Because the elements in  $\mathbf{X}_a$  (i.e.,  $X_{a,1}, X_{a,2}, \dots, X_{a,D}$ ) are weights and biases in an FNN in this research, smaller absolute values of  $X_{a,i}$  are preferable as initial values. Thus, the initial values for  $X_{a,i}$  are randomly sampled

from the normal distribution  $N(0, \varepsilon)$  or uniformly from an interval  $[-\varepsilon, \varepsilon]$  where  $\varepsilon$  is a small positive number. In the case of employing the [lower, upper] model (the LU model), two values are sampled per  $X_{a,i} = [x_{a,i}^L, x_{a,i}^U]$ : the smaller (larger) one is set to  $x_{a,i}^L$  ( $x_{a,i}^U$ ). In the case of employing the (center, width) model (the CW model), two values are sampled per  $X_{a,i} = (x_{a,i}^c, x_{a,i}^w)$ : one of the two values is set to  $x_{a,i}^c$  and the absolute value of the other is set to  $x_{a,i}^w$ .

### B. Fitness Evaluation

To evaluate fitness of an FNN as a phenotype instance of the corresponding genotype instance  $\mathbf{X}_a = [X_{a,1}, X_{a,2}, \dots, X_{a,D}]$  where  $\mathbf{X}_a \in \{\mathbf{X}_1, \mathbf{X}_2, \dots, \mathbf{X}_P\}$ , the FNN is supplied with several samples of input real vectors and calculates output values. The input values are sampled within the variable domain of application problem. Fitness of the genotype instance  $\mathbf{X}_a$  is evaluated based on the output values. The method for scoring the fitness based on the output values depends on the problem to which the FNN is applied. For example, in a case where the FNN is applied to controlling an automated system, some performance measure of the system can be used as the fitness score of the genotype instance corresponding to the FNN.

### C. Updates of Particles

Let the position vector of a particle, its personal best and the global (or its local) best be denoted as  $\mathbf{X}_r$ ,  $\mathbf{Pbest}_r$ ,  $\mathbf{Gbest}$  (or  $\mathbf{Lbest}_r$ ). In the case of using the LU model,  $\mathbf{X}_r = [X_{r,1}, X_{r,2}, \dots, X_{r,D}]$  and  $X_{r,i} = [x_{r,i}^L, x_{r,i}^U]$ . Let the velocity for  $x_{r,i}^L$  and  $x_{r,i}^U$  be denoted as  $v1_{r,i}$  and  $v2_{r,i}$  respectively. Note that  $v1_{r,i}$  ( $v2_{r,i}$ ) is not the lower (upper) limit of an interval so that  $v2_{r,i}$  can be smaller than  $v1_{r,i}$ .  $v1_{r,i}$  and  $v2_{r,i}$  are updated as:

$$v1_{r,i} = wv1_{r,i} + c_1r_1(pb_{r,i}^L - x_{r,i}^L) + c_2r_2(gb_{r,i}^L - x_{r,i}^L), \quad (9)$$

$$v2_{r,i} = wv2_{r,i} + c_1r_1(pb_{r,i}^U - x_{r,i}^U) + c_2r_2(gb_{r,i}^U - x_{r,i}^U), \quad (10)$$

employing the global best model, or as:

$$v1_{r,i} = wv1_{r,i} + c_1r_1(pb_{r,i}^L - x_{r,i}^L) + c_2r_2(lb_{r,i}^L - x_{r,i}^L), \quad (11)$$

$$v2_{r,i} = wv2_{r,i} + c_1r_1(pb_{r,i}^U - x_{r,i}^U) + c_2r_2(lb_{r,i}^U - x_{r,i}^U), \quad (12)$$

employing the local best model. The constant values  $w$ ,  $c_1$ ,  $c_2$  and the random values  $r_1$ ,  $r_2$  are the same as those in the ordinary PSO with the real-valued genotypes.

Similarly, in the case of using the CW model,  $X_{r,i} = (x_{r,i}^c, x_{r,i}^w)$  and  $v1_{r,i}$  and  $v2_{r,i}$  are the velocity for  $x_{r,i}^c$  and  $x_{r,i}^w$  respectively.  $v1_{r,i}$  and  $v2_{r,i}$  are updated as:

$$v1_{r,i} = wv1_{r,i} + c_1r_1(pb_{r,i}^c - x_{r,i}^c) + c_2r_2(gb_{r,i}^c - x_{r,i}^c), \quad (13)$$

$$v2_{r,i} = wv2_{r,i} + c_1r_1(pb_{r,i}^w - x_{r,i}^w) + c_2r_2(gb_{r,i}^w - x_{r,i}^w), \quad (14)$$

employing the global best model, or as:

$$v1_{r,i} = wv1_{r,i} + c_1r_1(pb_{r,i}^c - x_{r,i}^c) + c_2r_2(lb_{r,i}^c - x_{r,i}^c), \quad (15)$$

$$v2_{r,i} = wv2_{r,i} + c_1r_1(pb_{r,i}^w - x_{r,i}^w) + c_2r_2(lb_{r,i}^w - x_{r,i}^w), \quad (16)$$

employing the local best model.

By using the updated  $v1_{r,i}$  and  $v2_{r,i}$ ,  $X_{r,i}$  is updated as:

$$x_{r,i}^L = x_{r,i}^L + v1_{r,i}, \quad (17)$$

$$x_{r,i}^U = x_{r,i}^U + v2_{r,i}, \quad (18)$$

or as:

$$x_{r,i}^c = x_{r,i}^c + v1_{r,i}, \quad (19)$$

$$x_{r,i}^w = x_{r,i}^w + v2_{r,i}. \quad (20)$$

Note that  $x_{r,i}^L$  must not be larger than  $x_{r,i}^U$  because  $x_{r,i}^L$  and  $x_{r,i}^U$  are the lower and upper limits of the fuzzy number  $X_{r,i}$ . Similarly,  $x_{r,i}^w$  must not be negative because  $x_{r,i}^w$  is the width of  $X_{r,i}$ . If the value of  $x_{r,i}^L$  becomes larger than the value of  $x_{r,i}^U$  after the updates by (17) and (18), these values must be repaired to meet the constraint. The repair method can be as follows:

- the value of  $x_{r,i}^U$  is assigned to  $x_{r,i}^L$ ,
- the value of  $x_{r,i}^L$  is assigned to  $x_{r,i}^U$ ,
- the mean value of  $x_{r,i}^L$  and  $x_{r,i}^U$  is calculated and assigned to both of  $x_{r,i}^L$  and  $x_{r,i}^U$ , or
- the two values for  $x_{r,i}^L$  and  $x_{r,i}^U$  are switched.

Similarly, if the value of  $x_{r,i}^w$  becomes negative after the updates by (20), the value must be repaired to meet the constraint. The repair method can be as follows:

- the value of  $x_{r,i}^w$  is assigned to 0, or
- the absolute value of  $x_{r,i}^w$  is assigned to  $x_{r,i}^w$ .

## 4. APPLICATION TO EVOLVING FUZZY NEURAL NETWORKS

The author experimentally evaluates the ability of the proposed FPSO by applying it to evolution of FNNs, in the same manner as in [6]. The FNNs are challenged to model hidden fuzzy functions. The author adopts the same two functions [6] as the targets for FNNs to model so that the author can compare the experimental result with that by the fuzzy GA [6]. For simplicity, the input  $x$  of the



target functions is not a real vector but a real scalar (so that the FNN includes only a single input unit) and  $0 \leq x \leq 1$ , as in the literature [1]. The outputs of the target functions are symmetric triangular fuzzy numbers. The functions  $F_1(x) = [F_1(x)^L, F_1(x)^U]$  and  $F_2(x) = [F_2(x)^L, F_2(x)^U]$  are as follows:

$$F_1(x)^L = 0.2\sin(2\pi x) - 0.1x^2 + 0.4, \quad (21)$$

$$F_1(x)^U = 0.2\sin(2\pi x) + 0.1x^2 + 0.6. \quad (22)$$

$$F_2(x)^L = 0.2\sin(2\pi x) + 0.2x^2 + 0.2, \quad (23)$$

$$F_2(x)^U = 0.2\sin(2\pi x) - 0.2x^2 + 0.7. \quad (24)$$

Figs.4 and 5 show these two functions, where:

- F0.0L and F0.0U denote  $F(x)^L$  and  $F(x)^U$ , i.e., the lower and upper limits of the support interval of  $F(x)$ ,
- F0.5L and F0.5U denote the lower and upper limits of the 0.5-level interval of  $F(x)$ , i.e.,  $F(x)|_{0.5}$ , and
- F1.0 denotes the peak of  $F(x)$ , i.e.,  $F(x)|_{1.0}$ .

The FNN is designed as follows [6]:

- Number of units: 1 input, 10 hidden, 1 output.
- $-10.0 \leq x_{r,i}^L, x_{r,i}^U, x_{r,i}^c \leq 10.0$ .

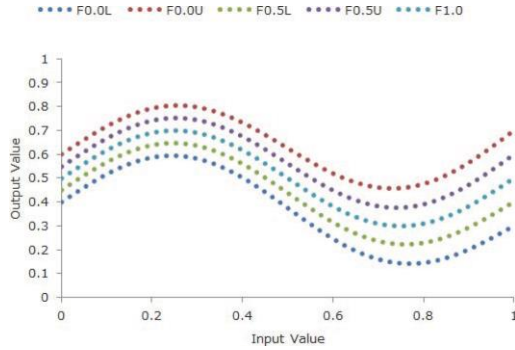


Figure 4. Target Function  $F_1(x)$  [6].

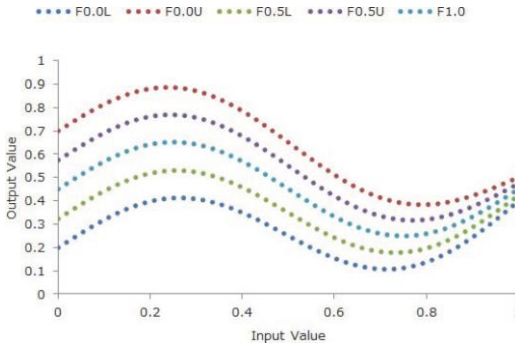


Figure 5. Target Function  $F_2(x)$  [6].

- $0.0 \leq x_{r,i}^w \leq 10.0$ .

The FPSO is designed as follows:

- Total number of FNNs evolved in a single run: 1,000,000.
- Population size and number of iterations: (100, 10,000), (500, 2,000)
- $w = 0.9, c_1 = 1.4, c_2 = 1.4$ .
- Initial values of  $x_{r,i}^L, x_{r,i}^U, x_{r,i}^c$  for the fuzzy weights and biases: uniformly random within  $[-1.0, 1.0]$ .
- Initial values for  $x_{r,i}^w$ : uniformly random within  $[0.0, 1.0]$ .
- Initial values of  $v1_{r,i}, v2_{r,i}$ : 0.0.
- $-0.1 \leq v1_{r,i}, v2_{r,i} \leq 0.1$

The number of iterations is 10,000 (or 2,000) for the FPSO with 100 (or 500) particles so that the total number of FNNs evaluated in a single run is consistently 1,000,000 ( $= 100 \times 10,000 = 500 \times 2,000$ ).

Particles  $\mathbf{X}_1, \mathbf{X}_2, \dots, \mathbf{X}_p$  are ranked by utilizing the same error function as that in literature [1,6]. As the values for the h-level intervals of fuzzy numbers, the author employs  $h = 0.2, 0.4, \dots, 1.0$  in this experiment. A phenotype instance FNN which corresponds to a genotype instance  $\mathbf{X}_i$  is supplied with a real input value  $x_r$  and calculates its output fuzzy number  $O_r$ .  $x_r$  is sampled within the input domain  $[0, 1]$  as  $x_r = 0.0, 0.01, 0.02, \dots, 1.0$ . Besides, each value of  $x_r$  is supplied to the target function  $F(x)$  and the output fuzzy number  $F(x_r)$  is obtained. Then, the cost  $e_r$  for the input  $x_r$  is calculated as:

$$e_r = \sum_h h((o_{r,h}^L - f_{r,h}^L)^2 + (o_{r,h}^U - f_{r,h}^U)^2), \quad (25)$$

where,

- $o_{r,h}^L$  and  $o_{r,h}^U$  are the lower and upper limits of the h-level interval of  $O_r$ , i.e.,  $O_r|_h = [o_{r,h}^L, o_{r,h}^U]$ , and
- $f_{r,h}^L$  and  $f_{r,h}^U$  are the lower and upper limits of the h-level interval of  $F(x_r)$ , i.e.,  $F(x_r)|_h = [f_{r,h}^L, f_{r,h}^U]$ .

For each genotype instance  $\mathbf{X}_i$ ,  $e_r$  is calculated 101 times ( $e_0, e_1, \dots, e_{100}$ ) for the 101 input values  $x_r = 0.0, 0.01, 0.02, \dots, 1.0$ , and the sum of  $e_r$  is used for ranking  $\mathbf{X}_i$ . An instance with a smaller sum of  $e_r$  is ranked better. Note that  $e_r$  scores are not utilized for calculating the values of updating the weights and biases but only for determining  $\mathbf{Pbest}_r$  and  $\mathbf{Gbest}$  (or  $\mathbf{Pbest}_r$  and  $\mathbf{Lbest}_r$ ).

Figs.6 and 7 show the results of this experiment. Fig.6 shows the output fuzzy function of the best FNN among the total 20,000,000 FNNs ( $= [1,000,000 \text{ FNNs in each run}] \times [\text{five runs}] \times [\text{two variations for population}$

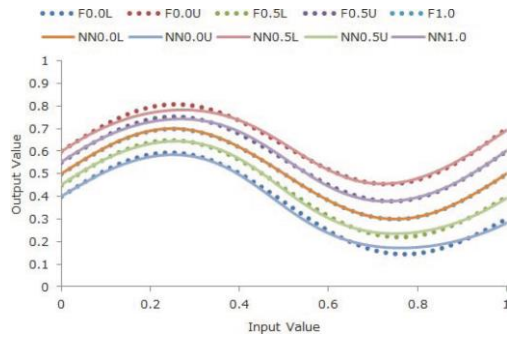


Figure 6. Output fuzzy function of the best FNN evolved by FPSO for modeling  $F_1(x)$ .

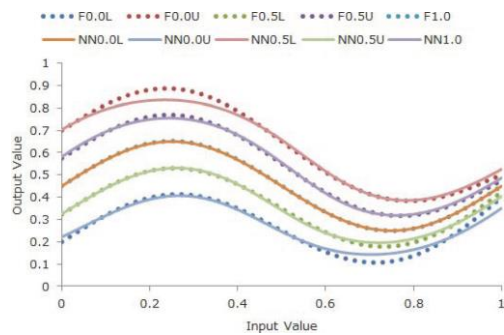


Figure 7. Output fuzzy function of the best FNN evolved by FPSO for modeling  $F_2(x)$ .

sizes]×[two variations for the interval model]) evolved by the FES for modeling  $F_1(x)$ . Fig.7 shows those for modeling  $F_2(x)$  in the same manner as Fig.6. In Figs.6 and 7,

- F0.0L, F0.0U, F0.5L, F0.5U and F1.0 are the same as those in Figs.4 and 5,
- NN0.0L and NN0.0U denote the lower and upper limits of the support interval of the FNN output fuzzy number,
- NN0.5L and NN0.5U denote the lower and upper limits of the 0.5-level interval of the FNN output fuzzy number, and
- NN1.0 denotes the peak of the FNN output fuzzy number.

Fig.8 shows the membership functions of  $O$  and  $F_1(x)$  for the input values  $x = 0.3$  and  $x = 0.7$ , where  $O$  is the output fuzzy number of the best FNN. In this figure,

- NN(0.3) and NN(0.7) show the membership functions of the output fuzzy number of the best FNN for the input values 0.3 and 0.7, while
- F(0.3) and F(0.7) show the membership functions of  $F_1(x)$  for the input values 0.3 and 0.7.

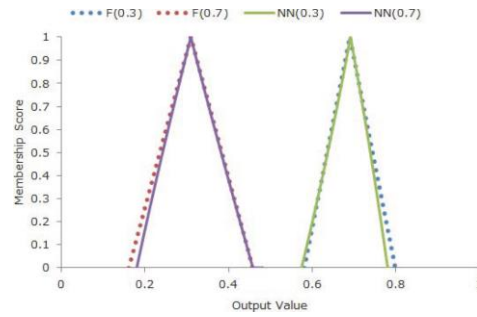


Figure 8. Output fuzzy numbers of the best FNN evolved by FPSO and target fuzzy numbers  $F_1(x)$  for the inputs values of 0.3 and 0.7.

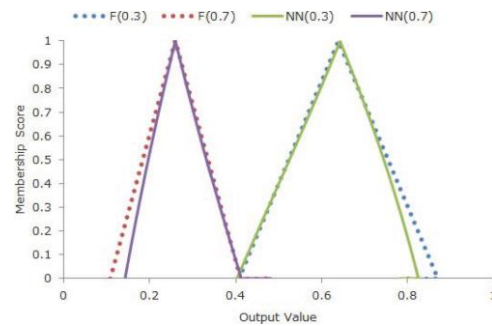


Figure 9. Output fuzzy numbers of the best FNN evolved by FPSO and target fuzzy numbers  $F_2(x)$  for the inputs values of 0.3 and 0.7.

Fig.9 shows those for  $F_2(x)$  in the same manner as Fig.8. The shapes of the FNN output fuzzy numbers (the solid curves in Figs.8 and 9) are similar to those of the target fuzzy numbers (the dotted lines in the same figures) for larger values of the membership score. These results shown in Figs.6-9 reveal that the best FNNs evolved by the FPSO approximate their target functions (especially for larger membership scores because the error is weighted more for the larger scores, see (25)), despite the fact that no training data is explicitly provided.

Fig.10 shows the error values of the best FNN for  $F_1(x)$  among each number of FNNs evolved (e.g., 500,000 FNNs are evolved in total at the 5,000th generation by the FPSO with 100 particles). In this figure, “FPSO” shows the result by FPSO proposed in this paper, and “FGA” shows the result by FGA [6]. The error values are the averaged ones over five runs. Fig.11 shows the error values for  $F_2(x)$  in the same manner as Fig.10. Figs.10 and 11 reveal that, for both of the two target functions, FGA contributed better than FPSO in evolving better FNNs: after the evolution of 1,000,000 FNNs, the dotted curves for FGA went below the solid curves for FPSO. This result will be because PSO tends to prematurely converge particles into a local minimum while GA can explore the search space well by the crossover and mutation operations. Although the result indicate FGA is superior to FPSO in evolving neural networks with fuzzy weights, several researchers have reported that PSO can outperform GA [22-26]. The author will further compare FPSO with FGA by applying them to

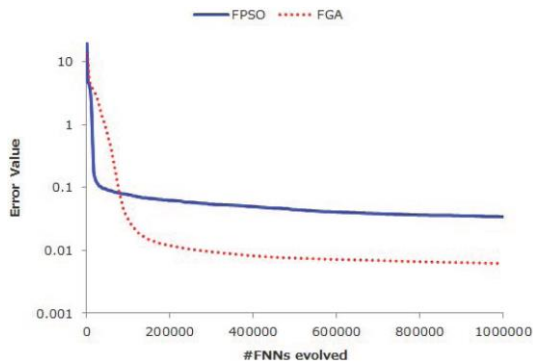


Figure 10. Error value of the best FNN at each number of FNNs evolved for modeling  $F_1(x)$ .

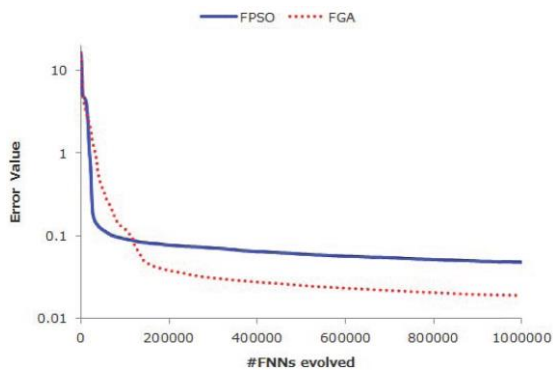


Figure 11. Error value of the best FNN at each number of FNNs evolved for modeling  $F_2(x)$ .

other fuzzy optimization problems, e.g., optimizing fuzzy if-then rules for fuzzy inference systems.

Besides, several methods have been proposed [27-32] for improving the traditional PSO. These improvements can be adopted to our FPSO. The author will evaluate how well these methods can improve our FPSO for solving fuzzy optimization problems.

## 5. CONCLUSION

In this paper, the author proposed the fuzzy-valued extension of PSO, and applied it to the evolution of neural networks with fuzzy weights and biases. In the proposed FPSO, genotype values are not real numbers but fuzzy numbers. To handle the fuzzy genotype values, the FPSO extends its processes of updating particles. The FPSO was challenged to evolve FNNs which model each of the two fuzzy functions. The experimental results showed that the best FNNs evolved by the FPSO approximated the target functions (especially for larger membership scores) despite the fact that no training data was explicitly provided.

In the future work, the author will further evaluate the ability of the FPSO by applying it to problems other than neuroevolution, e.g., evolving fuzzy if-then rules for fuzzy inference systems.

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